

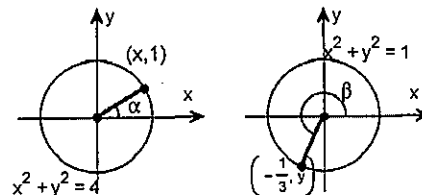
Student: \_\_\_\_\_  
Date: \_\_\_\_\_

Instructor: Joe Betters  
Course: Pre-Calculus Pre AP (Master Course)

Assignment: 7.5 Classwork (Day 1)

1. Use the figures to evaluate the function if  $f(x) = \tan x$ .

$$f(\alpha + \beta)$$



Choose the exact value of  $f(\alpha + \beta)$  below.

- A.  $f(\alpha + \beta) = -\frac{8\sqrt{2} + 9\sqrt{3}}{5}$
- B.  $f(\alpha + \beta) = -\frac{4\sqrt{2} + 7\sqrt{3}}{5}$
- C.  $f(\alpha + \beta) = \frac{8\sqrt{2} + 9\sqrt{3}}{5}$
- D.  $f(\alpha + \beta) = \frac{7\sqrt{3} - 4\sqrt{2}}{5}$

2. Establish the identity.

$$\frac{\cos(\alpha + \beta)}{\cos \alpha \cos \beta} = 1 - \tan \alpha \tan \beta$$

Choose the sequence of steps below that verifies the identity.

- A.  $\frac{\cos(\alpha + \beta)}{\cos \alpha \cos \beta} = \frac{\sin \alpha \sin \beta + \cos \alpha \cos \beta}{\cos \alpha \cos \beta} = \frac{\sin \alpha \sin \beta}{\cos \alpha \cos \beta} + \frac{\cos \alpha \cos \beta}{\cos \alpha \cos \beta} = 1 - \tan \alpha \tan \beta$
- B.  $\frac{\cos(\alpha + \beta)}{\cos \alpha \cos \beta} = \frac{\cos \alpha \cos \beta + \sin \alpha \sin \beta}{\cos \alpha \cos \beta} = \frac{\cos \alpha \cos \beta}{\cos \alpha \cos \beta} + \frac{\sin \alpha \sin \beta}{\cos \alpha \cos \beta} = 1 - \tan \alpha \tan \beta$
- C.  $\frac{\cos(\alpha + \beta)}{\cos \alpha \cos \beta} = \frac{\cos \alpha \cos \beta - \sin \alpha \sin \beta}{\sin \alpha \sin \beta} = \frac{\cos \alpha \cos \beta}{\sin \alpha \sin \beta} - \frac{\sin \alpha \sin \beta}{\sin \alpha \sin \beta} = 1 - \tan \alpha \tan \beta$
- D.  $\frac{\cos(\alpha + \beta)}{\cos \alpha \cos \beta} = \frac{\cos \alpha \cos \beta - \sin \alpha \sin \beta}{\cos \alpha \cos \beta} = \frac{\cos \alpha \cos \beta}{\cos \alpha \cos \beta} - \frac{\sin \alpha \sin \beta}{\cos \alpha \cos \beta} = 1 - \tan \alpha \tan \beta$

3. Find the exact value of the expression.

$$\sin \left( \sin^{-1} \frac{1}{2} + \cos^{-1} 0 \right)$$

$$\sin \left( \sin^{-1} \frac{1}{2} + \cos^{-1} 0 \right) = \underline{\hspace{2cm}}$$

(Simplify your answer. Type an exact answer, using radicals as needed. Use integers or fractions for any numbers in the expression.)

4. Find the exact value of the expression.

$$\cos \left[ \tan^{-1} \frac{40}{9} + \cos^{-1} \frac{4}{5} \right]$$

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$$\cos \left[ \tan^{-1} \frac{40}{9} + \cos^{-1} \frac{4}{5} \right] = \underline{\hspace{2cm}}$$

(Simplify your answer, including any radicals. Use integers or fractions for any numbers in the expression.)

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5. Solve the equation.

$$\cos \theta + \sqrt{3} \sin \theta = 1.$$

What is the solution in the interval  $0 \leq \theta < 2\pi$ ? Select the correct choice and fill in any answer boxes in your choice below.

A.  $\theta = \{ \underline{\hspace{2cm}} \}$

(Simplify your answer. Type an exact answer, using  $\pi$  as needed. Type your answer in radians. Use integers or fractions for any numbers in the expression. Use a comma to separate answers as needed.)

B. There is no solution.

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6. Show that the difference quotient for  $f(x) = \sin x$  is given by the following.

$$\begin{aligned} \frac{f(x+h) - f(x)}{h} &= \frac{\sin(x+h) - \sin x}{h} \\ &= \cos x \cdot \frac{\sin h}{h} - \sin x \cdot \frac{1 - \cos h}{h} \end{aligned}$$

Rewrite  $\sin(x+h)$ . Choose the correct answer below.

- A.  $\frac{\sin x \cos h - \sin h \cos x - \sin x}{h}$
- B.  $\frac{\sin x \sin h - \cos x \cos h - \sin x}{h}$
- C.  $\frac{\sin x \cos h + \sin h \cos x - \sin x}{h}$
- D.  $\frac{\sin x \sin h + \cos x \cos h - \sin x}{h}$

Rewrite the resulting expression.

- A.  $\frac{\sin h \cos x - \sin x(1 - \cos h)}{h}$
- B.  $\frac{\sin h \cos x + \sin x(1 - \cos h)}{h}$
- C.  $\frac{\cos x \cos h - \sin x(1 - \sin h)}{h}$
- D.  $\frac{\sin h \cos x + \sin x(1 + \cos h)}{h}$

Rewrite the resulting expression again.

- A.  $\frac{\sin h \cos x}{h} + \frac{\sin x(1 - \cos h)}{h}$
- B.  $\frac{\sin h \cos x}{h} - \frac{\sin x(1 - \cos h)}{h}$
- C.  $\frac{\sin h \cos x}{h} + \frac{\sin x(1 + \cos h)}{h}$
- D.  $\frac{\cos x \cos h}{h} - \frac{\sin x(1 - \sin h)}{h}$

Therefore, the difference quotient for  $f(x) = \sin x$  is  $\cos x \cdot \frac{\sin h}{h} - \sin x \cdot \frac{1 - \cos h}{h}$ .

1. A.  $f(\alpha + \beta) = -\frac{8\sqrt{2} + 9\sqrt{3}}{5}$

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2. D.  $\frac{\cos(\alpha + \beta)}{\cos \alpha \cos \beta} = \frac{\cos \alpha \cos \beta - \sin \alpha \sin \beta}{\cos \alpha \cos \beta} = \frac{\cos \alpha \cos \beta}{\cos \alpha \cos \beta} - \frac{\sin \alpha \sin \beta}{\cos \alpha \cos \beta} = 1 - \tan \alpha \tan \beta$

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3.  $\frac{\sqrt{3}}{2}$

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4.  $-\frac{84}{205}$

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5. A.  $\theta = \left\{ 0, \frac{2\pi}{3} \right\}$

(Simplify your answer. Type an exact answer, using  $\pi$  as needed. Type your answer in radians. Use integers or fractions for any numbers in the expression. Use a comma to separate answers as needed.)

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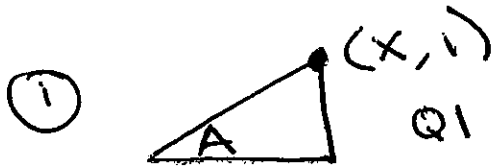
6. C.  $\frac{\sin x \cos h + \sin h \cos x - \sin x}{h}$

A.  $\frac{\sin h \cos x - \sin x(1 - \cos h)}{h}$

B.  $\frac{\sin h \cos x}{h} - \frac{\sin x(1 - \cos h)}{h}$

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# 7.5 classwork day 1



$$x^2 + y^2 = 4$$

$$x^2 + (1)^2 = 4$$

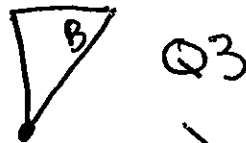
$$x^2 = 3$$

$$x = \sqrt{3}$$

$$y = 1$$

$$r = 2$$

$$\tan A = \frac{1}{\sqrt{3}}$$



$$(-1/3, y)$$

$$x^2 + y^2 = 1$$

$$(-1/3)^2 + y^2 = 1$$

$$y^2 = \frac{8}{9}$$

$$y = -\frac{2\sqrt{2}}{3}$$

$$x = -1/3$$

$$y = -\frac{2\sqrt{2}}{3}$$

$$r = 1$$

$$\tan B = \frac{-\frac{2\sqrt{2}}{3}}{-1/3}$$

$$\tan B = 2\sqrt{2}$$

$$\tan(A+B) = \frac{\tan A + \tan B}{1 - \tan A \tan B}$$

$$= \frac{\frac{1}{\sqrt{3}} + 2\sqrt{2}}{1 - (\frac{1}{\sqrt{3}})(2\sqrt{2})}$$

$$= \frac{\frac{1}{\sqrt{3}} + 2\sqrt{2}}{1 - \frac{2\sqrt{2}}{\sqrt{3}}}$$

$$= \frac{8\sqrt{2} + 9\sqrt{3}}{5}$$

A

## 7.5 classwork day 1 continued

$$\textcircled{2} \frac{\cos(A+B)}{\cos A \cos B} = 1 - \tan A \tan B$$

\* Formula

$$\frac{\cos A \cos B - \sin A \sin B}{\cos A \cos B} =$$

\* split

$$\frac{\cos A \cos B}{\cos A \cos B} - \frac{\sin A \sin B}{\cos A \cos B} =$$

$$1 - \tan A \tan B =$$

$\square$  D

## 7.5 classwork day 1 continued

$$\textcircled{3} \sin(\sin^{-1}(1/2) + \cos^{-1}(0))$$

$$* \sin \theta = 1/2$$

$$\theta = \boxed{\pi/6}$$

$$-\pi/2 \leq \theta \leq \pi/2$$

$$* \cos \theta = 0$$

$$\theta = \boxed{\pi/2}$$

$$3\pi/2$$

$$0 \leq \theta \leq \pi$$

↑  
outside  
parameter

$$\sin(\pi/6 + \pi/2)$$

\* Formula

$$\sin A \cos B + \cos A \sin B$$

$$\sin \pi/6 \cos \pi/2 + \cos \pi/6 \sin \pi/2$$

$$\left(\frac{1}{2}\right)(0) + \frac{\sqrt{3}}{2}(1)$$

$$= \boxed{\frac{\sqrt{3}}{2}}$$

$$* \sin(\pi/6 + \pi/2)$$

$$\sin(2\pi/3)$$

$$\frac{\sqrt{3}}{2}$$

# 7.5 classwork day 1 continued

$$\textcircled{4} \cos \left[ \tan^{-1} \left( \frac{40}{9} \right) + \cos^{-1} \left( \frac{4}{5} \right) \right]$$

$$\frac{A}{\tan \theta = \frac{40}{9} = \frac{y}{x}}$$

$$x^2 + y^2 = r^2$$

$$(9)^2 + (40)^2 = r^2$$

$$\sin \theta = \frac{y}{r} = \frac{40}{41}$$

$$r = 41$$

$$\cos \theta = \frac{x}{r} = \frac{9}{41}$$

$$\frac{B}{* \cos \theta = \frac{4}{5} = \frac{x}{r}}$$

$$x^2 + y^2 = r^2$$

$$(4)^2 + y^2 = 5^2$$

$$y = 3$$

$$\sin \theta = \frac{3}{5}$$

$$\cos \left( \frac{9}{41} + \frac{4}{5} \right)$$

\* Formula

$$\cos A \cos B - \sin A \sin B$$

$$\left( \frac{9}{41} \right) \left( \frac{4}{5} \right) - \left( \frac{40}{41} \right) \left( \frac{3}{5} \right) =$$

$$\boxed{\frac{-84}{205}}$$



## 7.5 classwork day 1 continued

$$\textcircled{5} \quad \cos \theta + \sqrt{3} \sin \theta = 1$$

$$\sqrt{1 - \sin^2 \theta} + \sqrt{3} \sin \theta = 1$$

$$\sqrt{1 - \sin^2 \theta} = 1 - \sqrt{3} \sin \theta$$

\* square both sides

$$1 - \sin^2 \theta = 1 - 2\sqrt{3} \sin \theta + 3 \sin^2 \theta$$

$$0 = 4 \sin^2 \theta - 2\sqrt{3} \sin \theta$$

$$0 = 2 \sin \theta (2 \sin \theta - \sqrt{3})$$

$$\sin \theta = 0$$

$$\sin \theta = \frac{\sqrt{3}}{2}$$

$$\theta = \{0, \pi\}$$

$$\theta = \left\{ \frac{\pi}{3}, \frac{2\pi}{3} \right\}$$

$$\theta = \{0, 2\pi/3\}$$

\*  $\pi$  and  $\frac{\pi}{3}$  do not work when plugged into original equation

7.5 classwork day 1 continued

⑥

$$\frac{\sin(x+h) - \sin x}{h}$$

\* use composite Argument property

$$\frac{\sin x \cosh + \cos x \sinh - \sin x}{h}$$

C

\* group ~~sin x~~  
sin x

$$\frac{\cos x \sinh - \sin x (1 - \cosh)}{h}$$

A

\* split common denominator

$$\frac{\sinh \cos x}{h} - \frac{\sin x (1 - \cosh)}{h}$$

B